

# Collections

## Directions:

You may use the Collections handouts to answer each part of this question. This practice question was from the 2016 SL Paper 1. You may check your answers with a partner but each student should complete each part of the question.

A local charity organizes a half-marathon to raise money. The rules to participate in the half-marathon are as follows:

- The organizers limit the total number of participants to 450
- Participants belong to a team and each team must have at least three and at most five participants
- Each participant registers for the event independently from the other members of their team, and they all declare their team name when registering
- For scoring, the team's final time is the sum of the times of its three fastest participants. Participants that do not cross the finishing line within 2 hours after the start, are assigned a default time of 1000 minutes. The **winning team** is the team with the smallest sum total.

During registration, an array, `PARTICIPANTS`, with 450 positions is used to hold the abbreviated team names that are declared by each participant. Simultaneously, a collection `TNAMES` is generated: any **new** team name that is declared is added to the collection.

- (a) State the minimum size of `TNAMES` to ensure the names of all potential teams can be stored. [1]

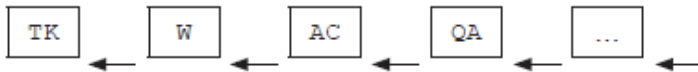
# Collections

Part of the array `PARTICIPANTS` is shown below, where, for example, the first participant declared that they are part of team `TK`. The initial part of the collection `TNAMES` is also shown, with arrows indicating the direction of growth.

`PARTICIPANTS`

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]	[10]	[11]	[12]	[13]	[14]	...
TK	W	AC	TK	W	TK	AC	W	TK	TK	AC	QA	AC	W	AC	...

`TNAMES`



Both `PARTICIPANTS` and `TNAMES` are used to construct the array, `TEAM`, that groups all participants who belong to the same team. Part of the array `TEAM` is shown below.

`TEAM`

[0]	[1]	[2]	[3]	[4]	[5]	[6]	[7]	[8]	[9]	[10]	[11]	[12]	[13]	[14]	...
3	4	6	5	7	8	10	13	9	0	12	73	14	15	2	...

Arrows in the original image point from index 3 to 0, 5 to 3, and 8 to 5, forming a path 0 → 3 → 5 → 8 → 9 → 0.

In `TEAM`, each **element** is related to one other **index** in the array, shown by the arrows on the above diagram. This relation will eventually form a closed path (for this example 0, 3, 5, 8, 9 and back to 0). The relation reflects the information in `PARTICIPANTS`, by grouping people who declared the same team name during registration.

Hence, participants 0, 3, 5, 8 and 9 are on the same team and, from `PARTICIPANTS`, that team is `TK`.

- (b) Identify the position in `PARTICIPANTS` of the second participant that registered for team `QA`.

[1]

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Part of the algorithm that generates the `TEAM` array is shown below, in pseudocode.

```
//Input PARTICIPANTS array, TNames collection
TEAM    // array with 450 positions, initialized to '999'
CURRENT // variable to store current name of team;
T, P    // variables to store the indexes of TEAM and PARTICIPANTS,
        // respectively;
MINP    // stores the first index P of members of the CURRENT team;

TNames.resetNext()
loop while TNames.hasNext()
    CURRENT = TName.getNext()
    T = 0; P = 0; MINP = 0    // variables' initialization
    /*
    /* Code to be completed in part (c) (i)
    /*
    /* Code to be completed in part (c) (ii)
    /*
end loop
output TEAM
```

(c) In order to complete this code, and return the correct `TEAM` array,

- (i) construct pseudocode to find `MINP`, the first index in `PARTICIPANTS` of the `CURRENT` team, and use it to start the construction of `TEAM` [3]
- (ii) construct pseudocode to find the other participants belonging to the `CURRENT` team, implementing the idea of the closed paths in the `TEAM` array. [4]

As part of the program to determine the winning team, an array, `TIMING`, is maintained in parallel to `PARTICIPANTS`. For example, `TIMING[5]` and `PARTICIPANTS[5]` relate to the same participant.

`TIMING` is initialized to zero before the race starts, and updated with the finishing times for each participant. The algorithm `sum3best` is able to output the sum of the three fastest times from any group of times that are passed to the algorithm.

- (d) Describe the steps of an algorithm that will find the **winning team**, as defined by the marathon rules on page 6. Clearly mention the use of existing or of new data structures. [6]